Monte Carlo Tree Search and Its Applications

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Kasparov vs Deep Blue



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Kasparov vs Deep Blue

Great display of artifical intelligence (AI) Techniques employed by IBM

- Brute force deterministic approach
- Human knowledge

Limitation

Scalability into larger search spaces

Monte Carlo tree search (MCTS) is an alternative method

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Outline

Introduction

Naive MCTS Implementation

Applying MCTS to Go

Applying MCTS to Narrative Generation

Conclusion

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Monte Carlo Tree Search (MCTS)

- Combines random sampling and game trees
- Lightweight random simulations
- Probabilistic not deterministic
- Useful for problems with larger search spaces

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Applying MCTS to Go

Go

- Board game about positional advantage
- Game board for Chess:
 - ► 8x8
- Average possible configurations for a game of Chess:
 - ► 10¹²⁰
- Game board for Go:
 - 19x19
- Average possible configurations for a game of Go:

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▶ 10⁷⁶¹

Applying MCTS to Narrative Generation

- Useful Applications
 - Video game replay value
 - Educational applications
- The search space scales with the number of characters, items, locations, and actions

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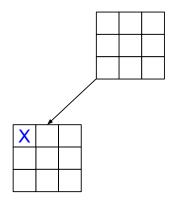
Applying MCTS to Narrative Generation

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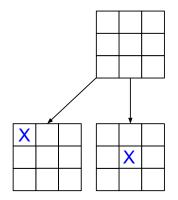
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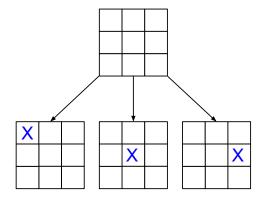
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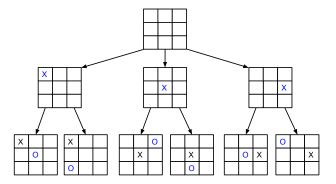


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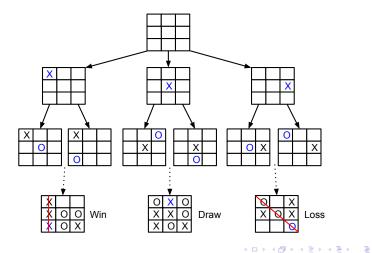
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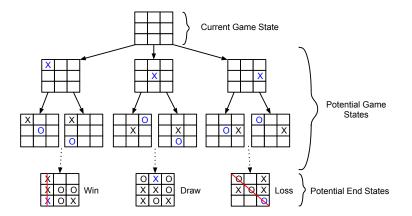
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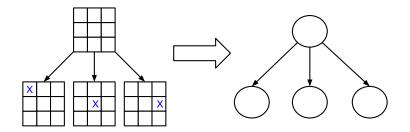


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Tree Structure

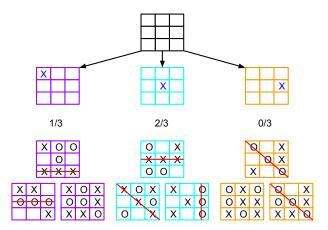


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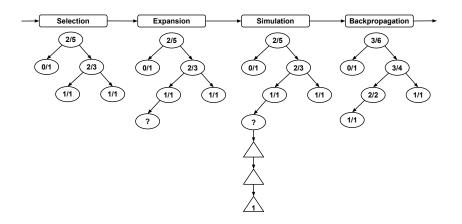
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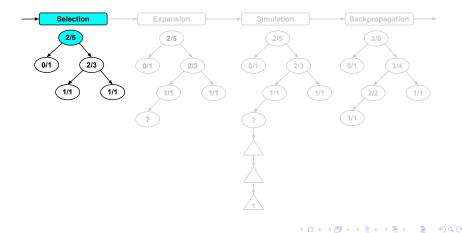
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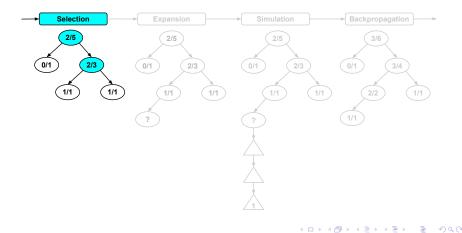
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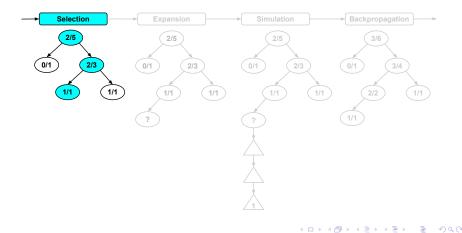
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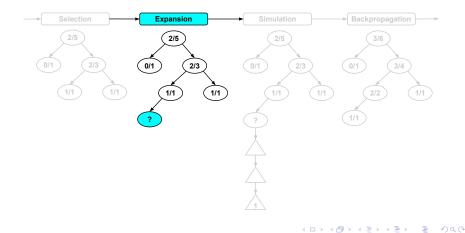
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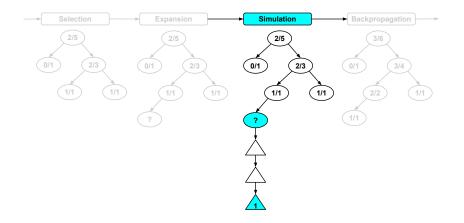
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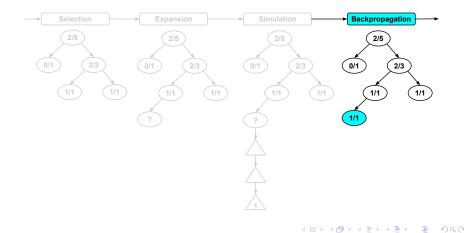
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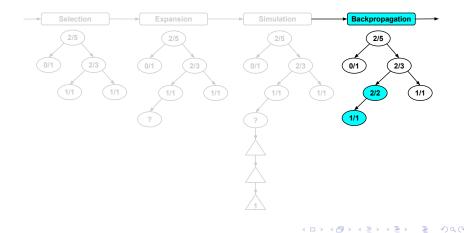
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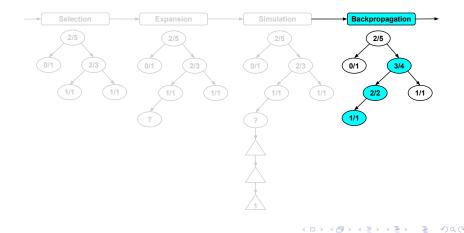
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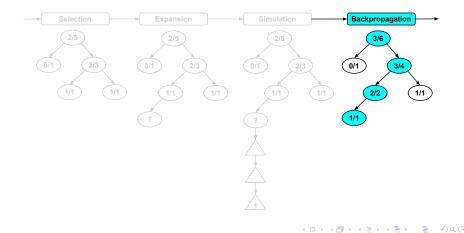
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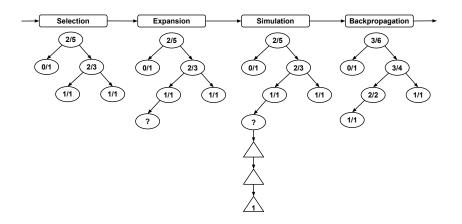
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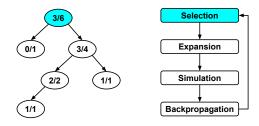
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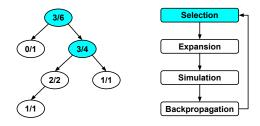
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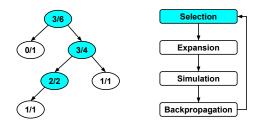
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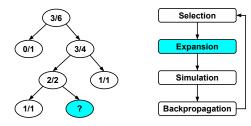
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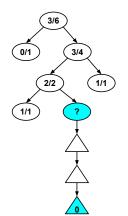
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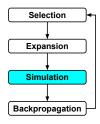


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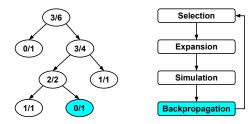




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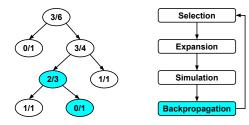
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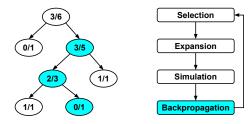
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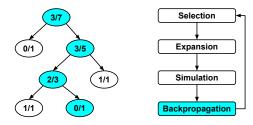
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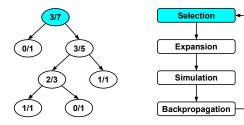
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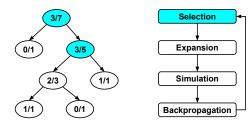
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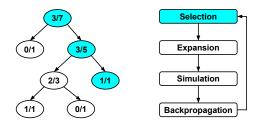
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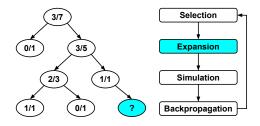
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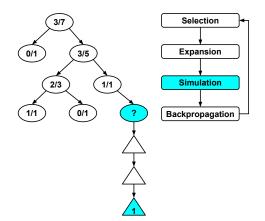
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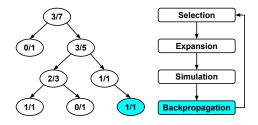
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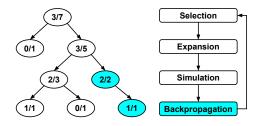
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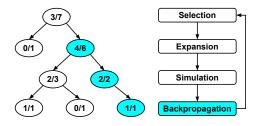
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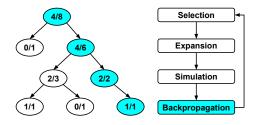
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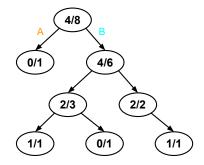
What Happens When We Choose a Move?

Now we have:

- A tree structure
- A method of generating the tree

What happens when we need to choose a move?

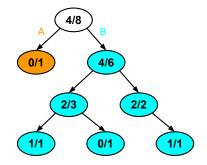
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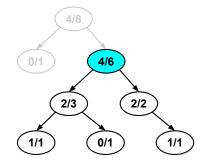
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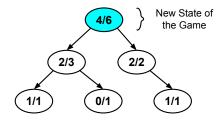
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Exploration vs Exploitation

- We might overlook better paths
- Exploration vs Exploitation
 - Exploration looks at more options
 - Exploitation focuses on the most promising path
- Must find a balance between the two

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Upper Confidence Bound Applied to Trees (UCT)

$$UCT(node) = \underbrace{\frac{W(node)}{N(node)}}_{Value of the Node} + \underbrace{\sqrt[c]{\frac{In(N(parentNode))}{N(node)}}}_{Exploration Bonus}$$

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- W represents the number of simulated wins
- N represents the total number of simulations
- C is an experimental constant
- Used during tree traversal
- Balances exploration vs exploitation

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Monte Carlo Tree Search and Its Applications

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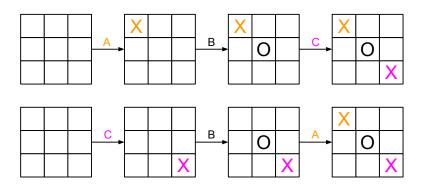
MCTS applied to Go

What variations can we make specific to Go? In Go each player takes turn placing pieces on a game board

- How much does the order of these moves matter?
- Can we use this to improve MCTS in the context of Go?

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Tree Redundancy



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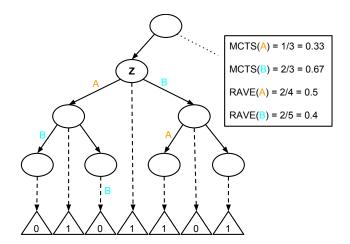
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Rapid Action Value Estimate (RAVE)

- Takes advantage of tree redundancy
- Moves have no contextual dependencies
- Stores the value of a move within a subtree at each node

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RAVE Diagram

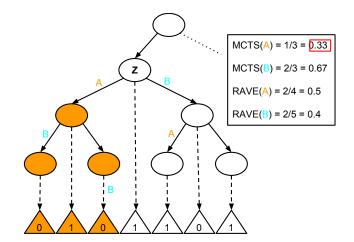


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MCTS Values

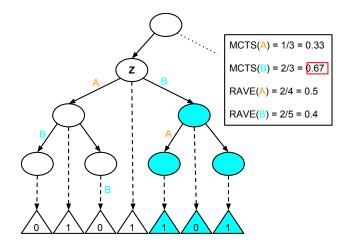


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MCTS Values

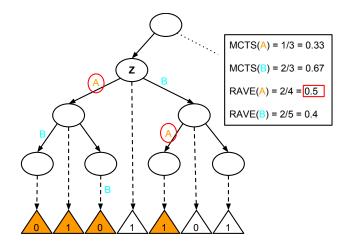


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RAVE Values

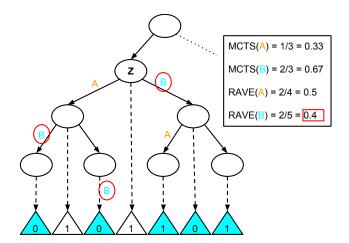


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RAVE Values

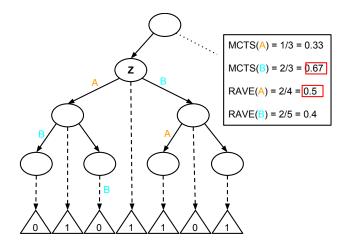


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MCTS RAVE Comparison



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RAVE

- Very powerful approach
- Each simulation provides us with more information
- Sometimes we do need contextual dependencies
 - Example: Close tactical battles

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MC RAVE

- Combines MCTS values with RAVE values
- Uses a weighted average
- Favors RAVE values when fewer simulations have been performed
 - Contextual dependencies are unknown
- Favors MCTS values when more simulations have been performed

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Contextual dependencies are more developed

Go Results

- Deterministic approaches could hardly defeat low level amateurs
- Computer Go programs use MC RAVE
 - MoGo
 - Crazy Stone
- Can compete against top pros in 9x9 Go
- Can compete against top pros in handicapped 19x19 Go

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Outline

Introduction

Naive MCTS Implementation

Applying MCTS to Go

Applying MCTS to Narrative Generation

Conclusion

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Narrative Generation

Kartal et al. applied MCTS to Narrative Generation

- Crime story
- User defines the set up and goals for the story
 - Example Setup: The detective starts in his office
 - Example Goal: The killer must be arrested

Unlike Go and other games

- Slightly different tree structure
- Evaluation function needed

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Actions

- Actions drive the story
- Actions are believable based on context
 - Example: Inspector searches for clues
 - Example: Character A kills Character B

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Example Actions

Move(A, P): A moves to place P. Kill(A, B): B's health to zero(dead). Earthquake(P): An earthquake strikes at place P.

- Actions take the place of moves
- No clear end state
- The researchers used a set threshold during simulation

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Evaluation function

- Method of giving nodes value
- Incorporates believability and goal completion
- Ensures stories are interesting
- Value(story) = Believability(story) * GoalCompletion(story)
 - Believability is the mathematical product of every action in a story

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The value is between 0 and 1

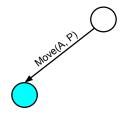
Narrative Generation Test

MCTS compared against three deterministic algorithms

- Breadth-first search
- Depth-first search
- Best-first search

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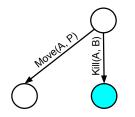
Breadth-First Search



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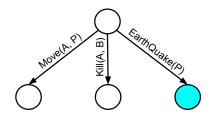
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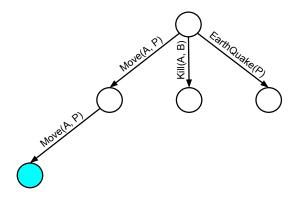
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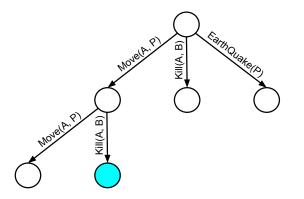
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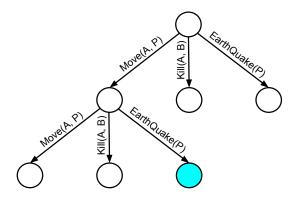
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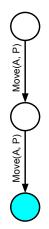
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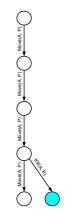
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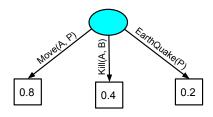
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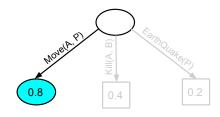
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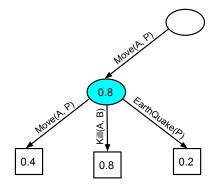
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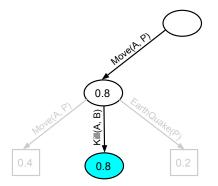
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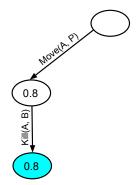
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Test Conditions

Goals for the narrative:

- At least two people are killed
- The killer is arrested
- Each algorithm was given two budgets
 - 100,000 nodes
 - 3 million nodes

Each algorithm ran three times The score of the narratives were averaged

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Results

	MCTS	Breadth- first	Depth- first	Best- first
Low Budget	0.07	0.05	<0.001	0.005
High Budget	0.9	0.06	<0.01	<0.01

- MCTS performed the best in both
- Breadth-first came the closest out of the deterministic algorithms

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Stories Produced by MCTS

- Stories from MCTS tended to be believable
- Completed both user defined goals
- Some problems
- Overall reasonable narratives

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Low Scoring Example from Breadth-First

Sherlock moved to Alice's House. An Earthquake occurred at Alice's House! Sherlock and Alice both died due to the earthquake.

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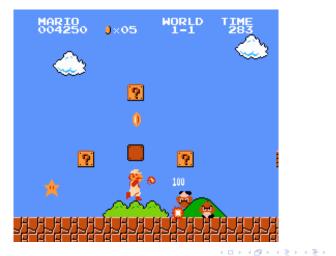
Conclusion

- MCTS successful in extending AI capabilities
- Tackles problems with larger search spaces
- Effective in Go and narrative generation
- Applicable to other problems
 - Can outperform humans in many puzzles
 - Real time games
 - Super Mario Brothers

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Any Questions?



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