
Electronic Voting System Implementation Through Bitcoin Blockchain Technology

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Electronic Voting

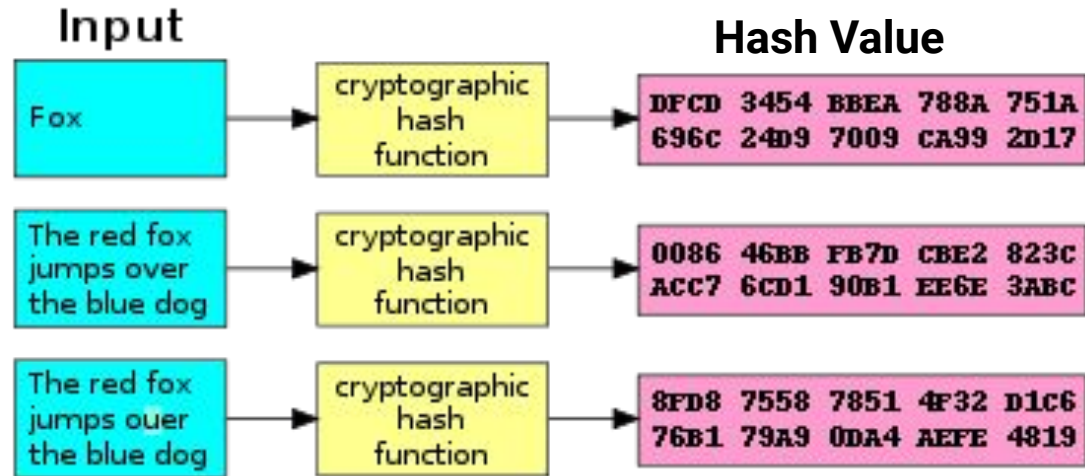
- Electronic voting (e-voting) is voting that uses electronics to aid in the voting process.
- Most voters use hand-marked paper ballots

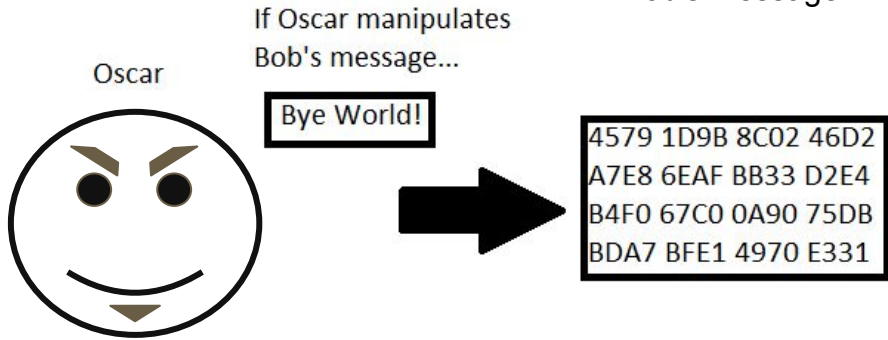
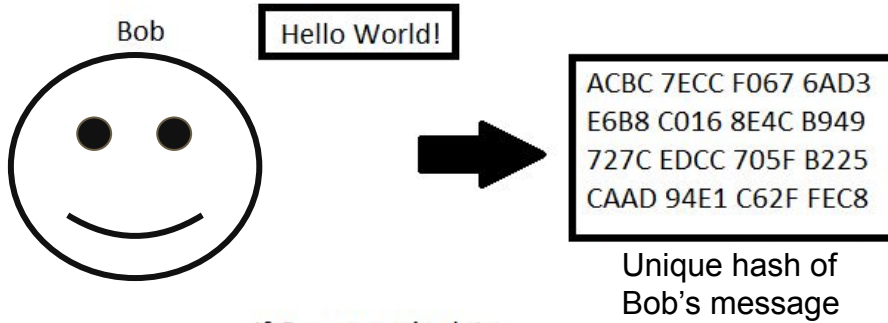
Outline

- Background Information
 - Cryptographically Secure Hash
 - Asymmetric Cryptography
 - Digital Signatures
 - Blind Signatures
 - Intro to Blockchain
- Using Blockchain for E-Voting
 - Pre-voting phase
 - Voting phase
 - Post-voting
- Practical considerations

Background - Cryptographically Secure Hash

- Mathematical algorithms that map data to a bit array
- Used to verify integrity message are unaltered.
- Easy to compute
- Impossible to reverse



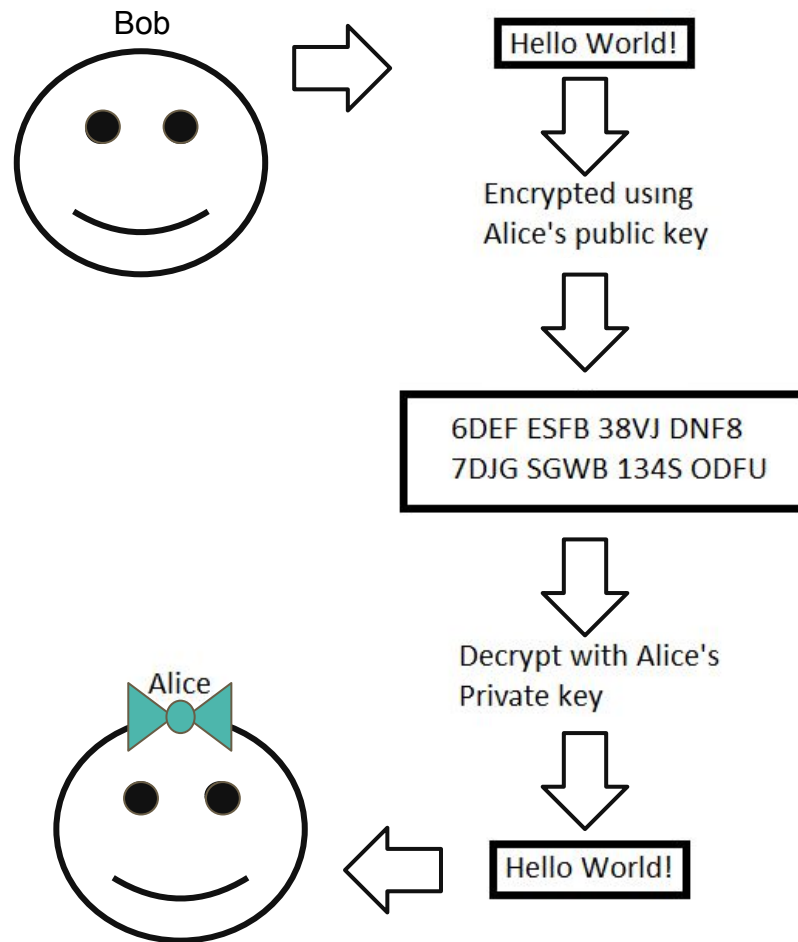


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Background- Asymmetric Cryptography

- Each participant gets a key pair
 - Private key, Public key
- Security relies on the private key staying private
- Public key only encrypts
- Private key decrypts



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Background - Digital Signatures

- Used to confirm the source, and the integrity of a message
- The goal of these signatures is not to hide the message

RSA Signatures - Key Generation

1. Two prime numbers p and q are chosen
2. Compute $n = pq$
 - a. n will be used as a modulus later on

1. $p = 61, q = 53$
2. $n = 61 * 53 = 3233$

RSA Signature Key Generation

-Euler's Phi Function

- For prime numbers, $\varphi(p) = p-1$
- multiplicative function:
 - $\varphi(pq) = \varphi(p)\varphi(q)$
 - $\varphi(pq) = (p-1)*(q-1)$
- $\varphi(n)$ will be used in subsequent steps

1. $p=61, q=53, n = p*q = 3233$

2. $\varphi(n)=60*52=3120$

RSA Signatures - Key Generation

Remember...

1. $p = 61, q = 53$
2. $n = 3233$
3. $\varphi(n) = 3120$

4. Choose integer e (Public Exponent)

5. Compute d (Private Exponent)

- $d * e \equiv 1 \pmod{\varphi(n)}$

Public key = (n, e)

Private key = (p, q, d)

4. $1 < e < \varphi(n)$, let $e = 17$

- $\text{GCD}(17, \varphi(n)) = 1$

5. $d = 413$

- $1 = (17 * 413) \pmod{3120}$

Public key = $(n = 3233, e = 17)$

Private key = $(p = 61, q = 53, d = 413)$

Signing A Message

- $h = \text{hash}(m)$;
- Alice attaches h^d as signature to message

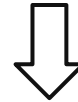


Hello World



Alice's creates a hash of her message

```
a591 a6d4 0bf4 2040
4a01 1733 cfb7 b190
d62c 65bf 0bcd a32b
57b2 77d9 ad9f 146e
```



Alice attaches the hash to her message as a 'signature'

Hello World

```
a591 a6d4 0bf4 2040
4a01 1733 cfb7 b190
d62c 65bf 0bcd a32b
57b2 77d9 ad9f 146e
```

Say $h = 65$,

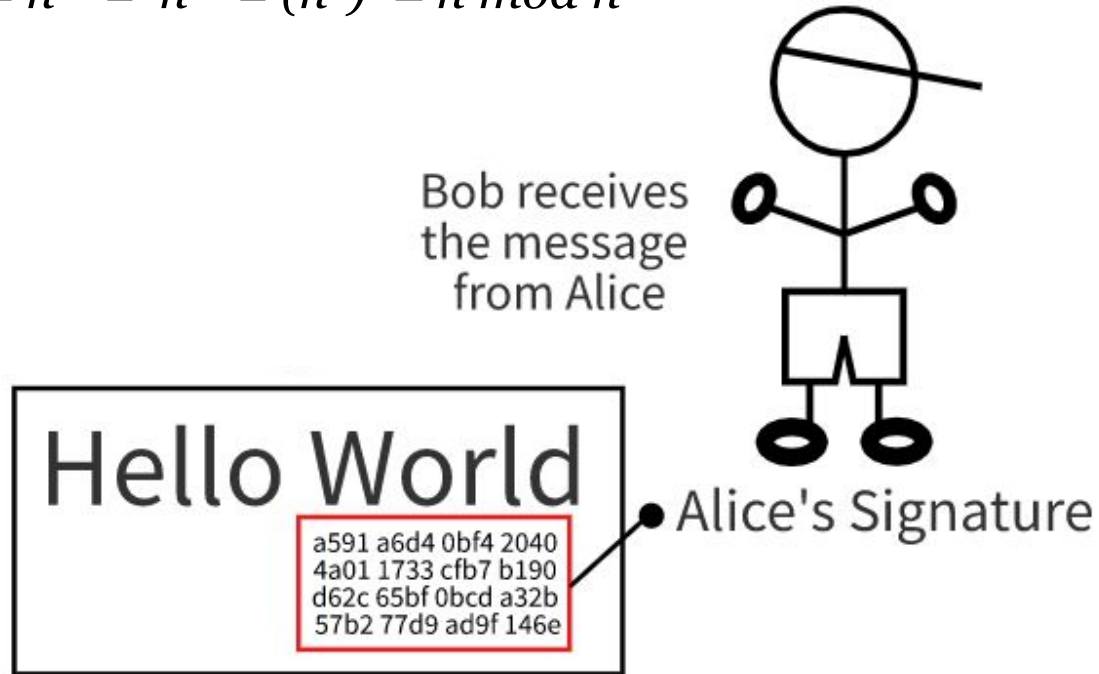
$h^d \pmod n = \text{Alice's Signature}$:

$65^{413} \pmod n = \text{Alice's Signature}$

Receiving A Signed Message

$$(h^e)^d = h^{ed} = h^{de} = (h^d)^e \equiv h \pmod n$$

- Bob raises Alice's signature value to the power of e
- Bob can then compare the hash value with Alice's hash value.



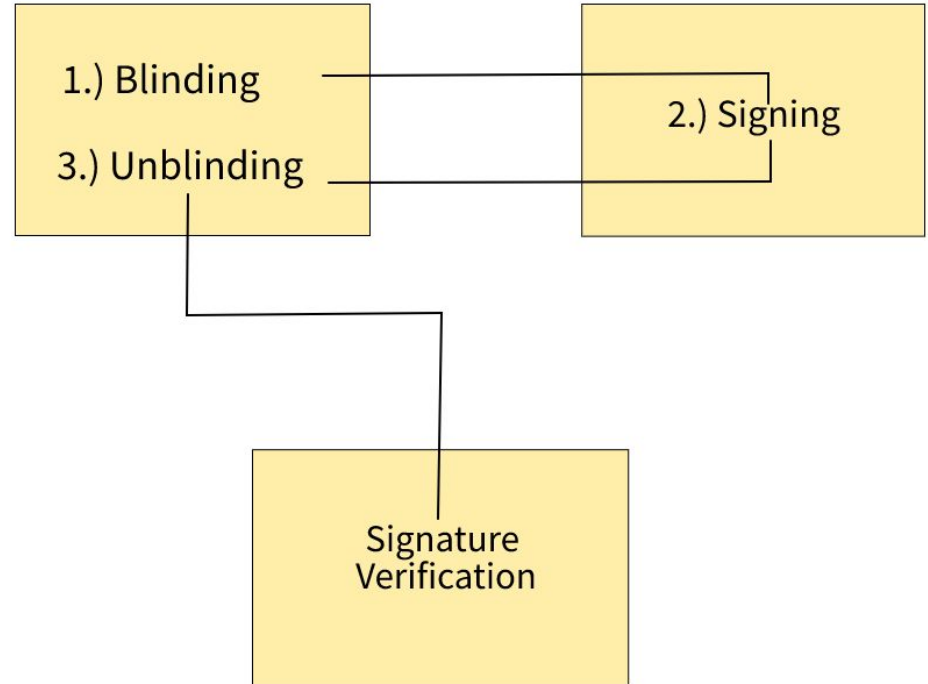
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Blind RSA Signatures

m' = blinded message
 s' = blind signature
 s = signature (unblinded)
 r^e = blinding factor

1. Send product of message and blinding factor
 - a. $m' = mr^e \pmod n$
2. Signer signs document
 - a. $s' = (m')^d \pmod n$
3. s' is sent back and blinding factor is removed
 - a.
$$\begin{aligned} s &= s' * r^{-1} \\ &= m^d * r^{ed} * r^{-1} \\ &= m^d * r * r^{-1} \\ &= m^d \end{aligned}$$

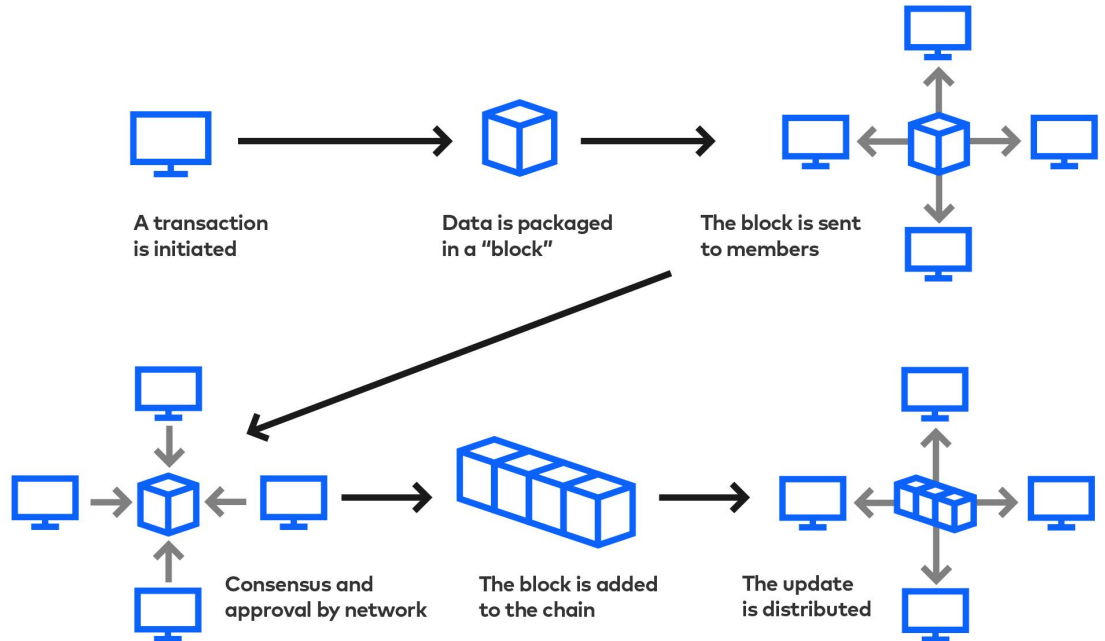


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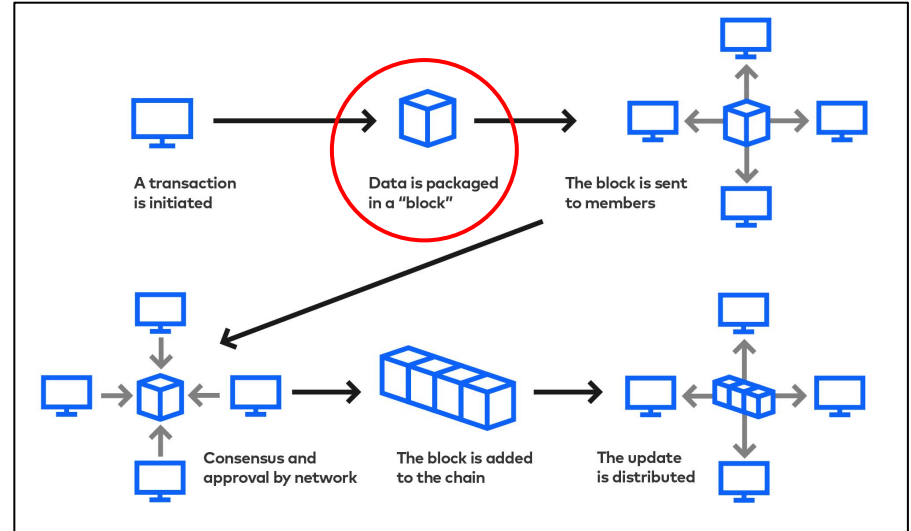
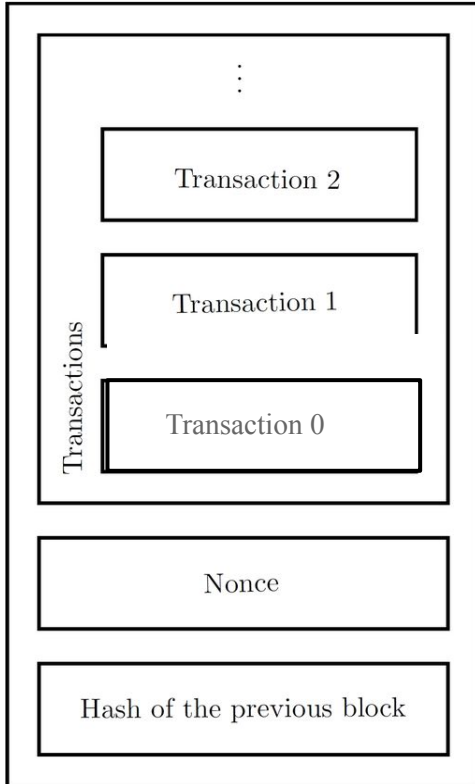
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Introduction to Blockchain

- Blockchain is a specific type of database (Distributed ledger)
- Blockchains store data in blocks that are then chained together
- Most common use so far has been as a ledger for transactions.



Introduction To Blockchain



- Nonce = number used once
- Each block holds the hash of the previous block

Proof of Work

"Hello, world!**0**" => 1312af178c253f84028d480a6adc1e25e81caa44c749ec81976192e2ec934c64
= $2^{252.253458683}$

"Hello, world!**1**" => e9afc424b79e4f6ab42d99c81156d3a17228d6e1eef4139be78e948a9332a7d8
= $2^{255.868431117}$

...

"Hello, world!**4248**" => 6e110d98b388e77e9c6f042ac6b497cec46660deef75a55ebc7cfd65cc0b965
= $2^{254.782233115}$

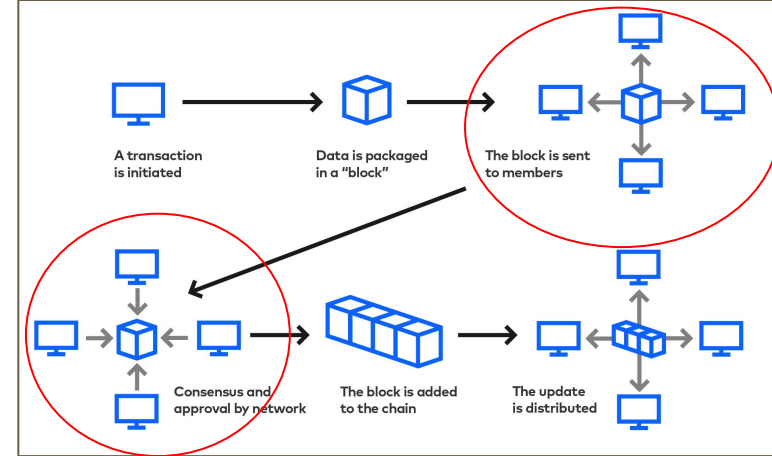
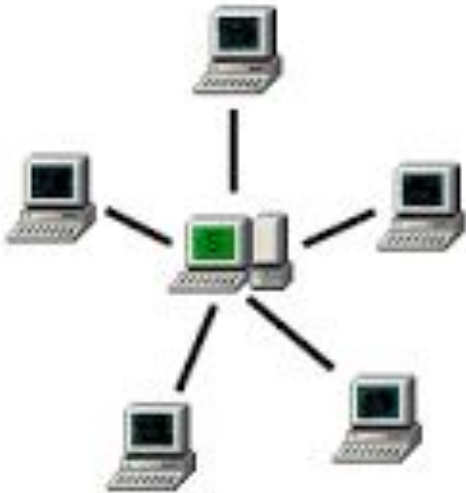
"Hello, world!**4250**" => 0000c3af42fc31103f1fdc0151fa747ff87349a4714df7cc52ea464e12dcd4e9
< **$2^{239.61238653}$**

Introduction to Blockchain- Peer-To-Peer Network

Server Based Network

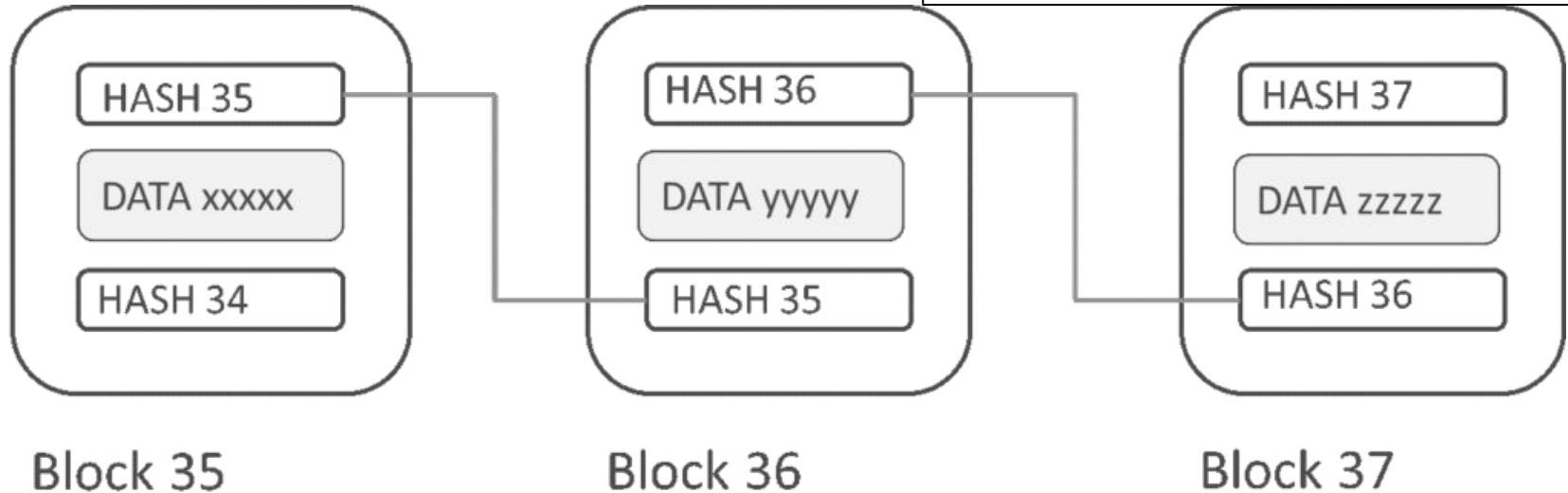
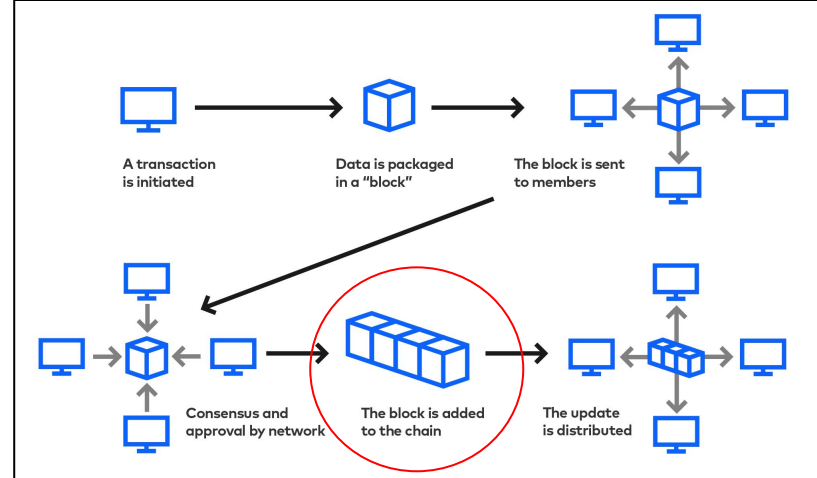
vs.

Peer-To-Peer Network



- Decentralized communication model
- Each device = a node
- All nodes hold equal power

Intro to Blockchain



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Using Blockchain for E-Voting

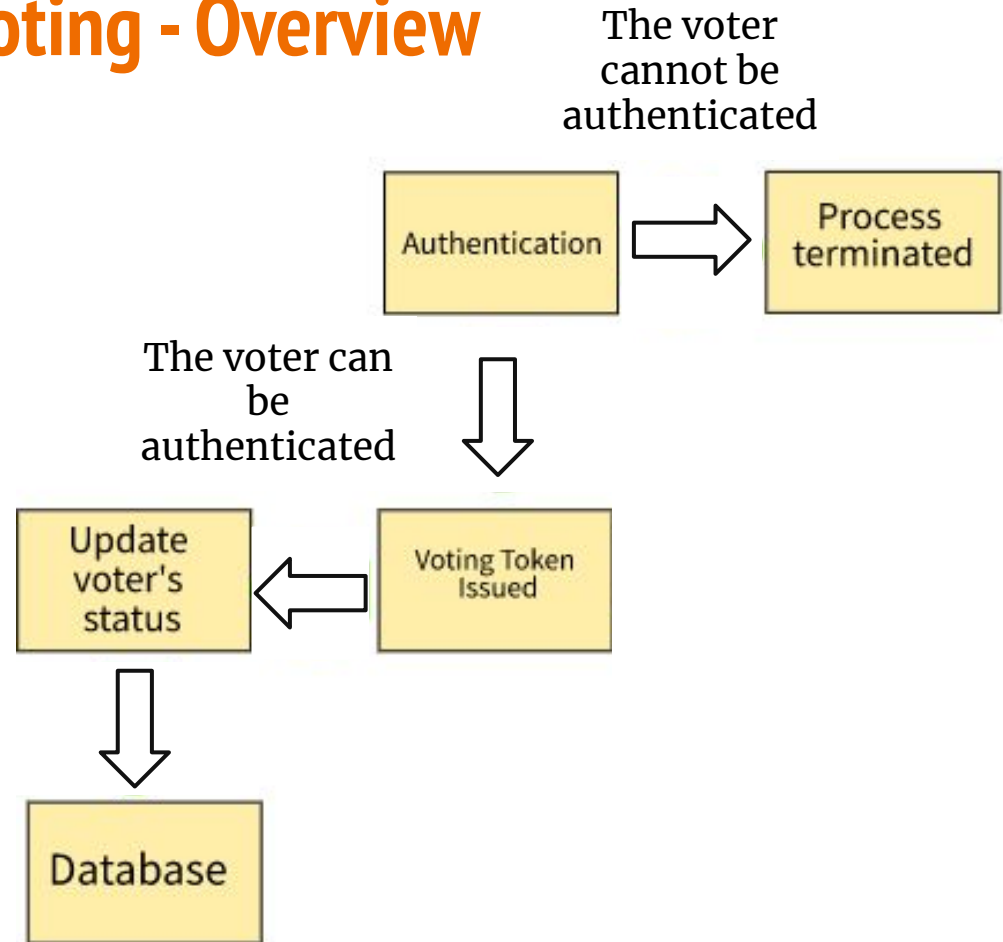
End-to-end Voting with Non-permissioned and Permissioned Ledgers:

Stefano Bistarelli · Ivan Mercanti · Paolo Santancini · Francesco Santin

- Published March 2020

Using Blockchain for E-Voting - Overview

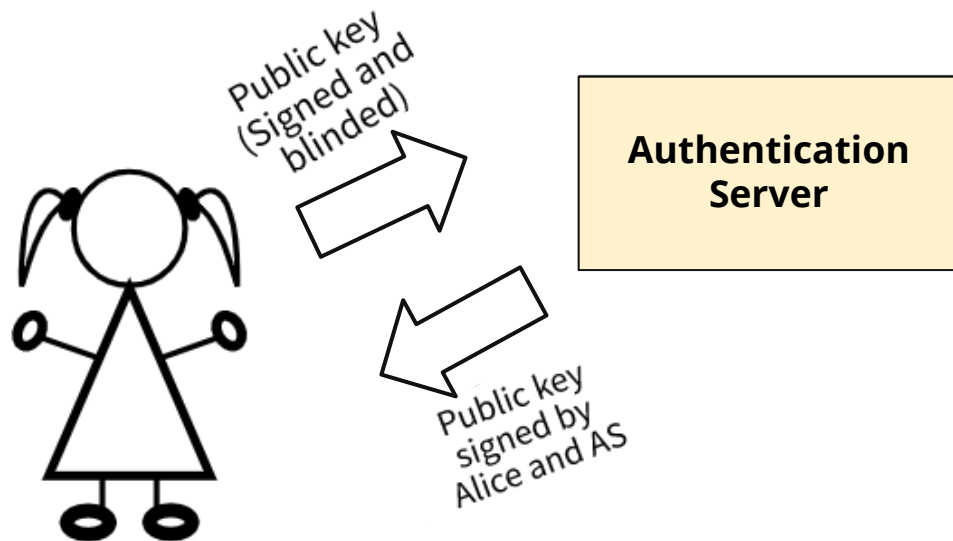
- Pre-Voting phase
 - Candidate nomination



Pre-voting Phase -Voter Authentication

Authentication Service (AS)

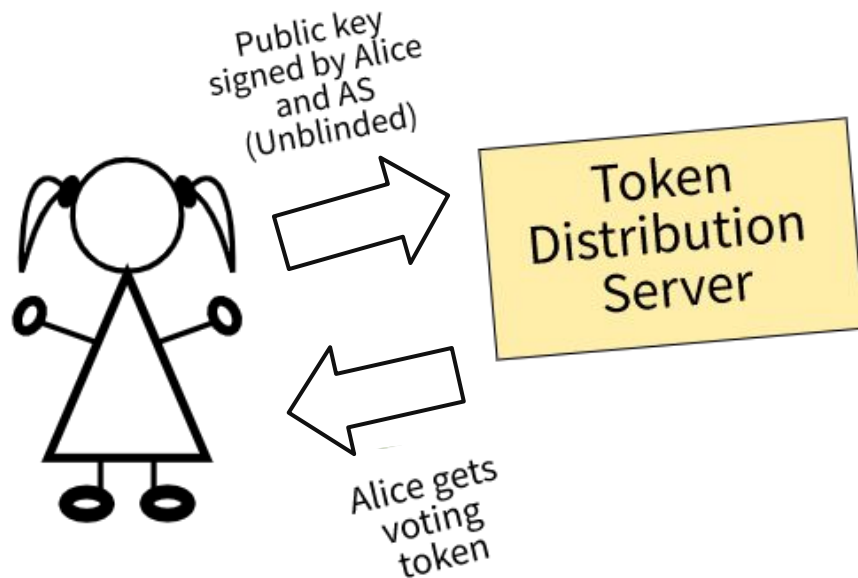
- Non-anonymous Authentication



Pre-Voting -Token Distribution

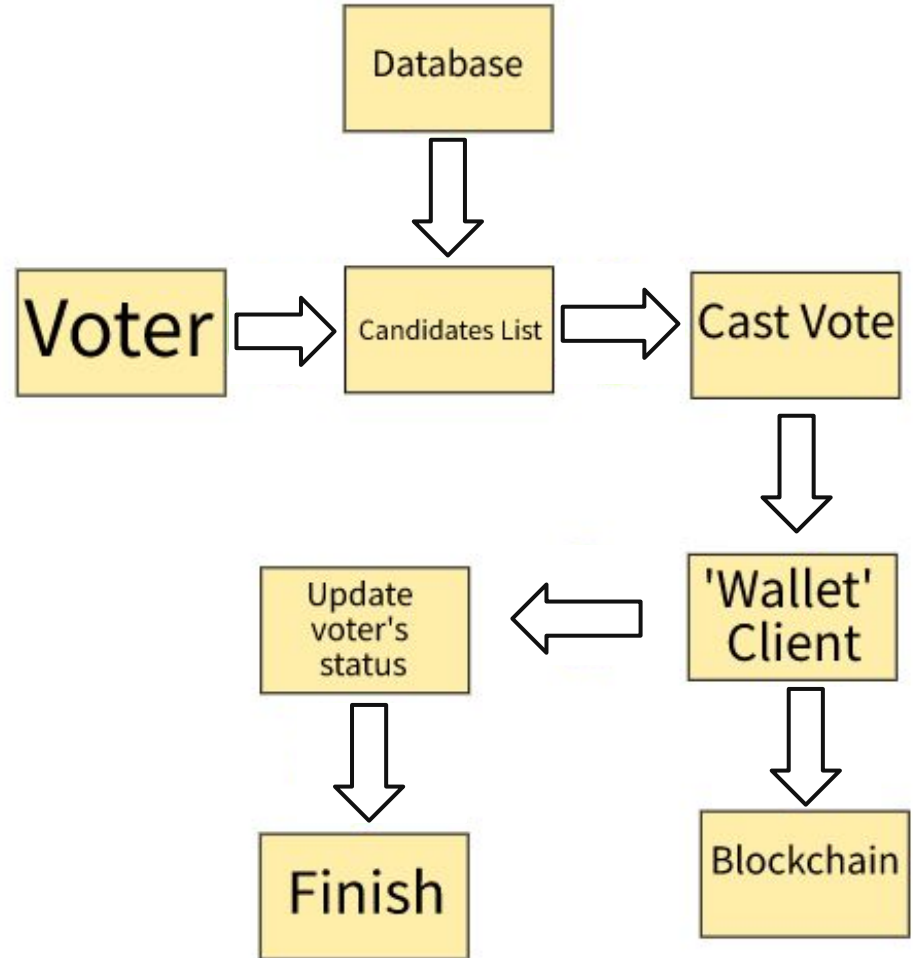
Token Distribution Service(TD)

- Anonymous distribution of tokens to Authenticated voters



Voting Phase

- Wallet within voting application hides the complicated aspects of the transactions from the user



Post Voting Phase

- Votes are counted by taking the sum of tokens received by each candidate
- Votes can be verified using permanently stored source information

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Practical Considerations

- Other countries have experimented with internet voting
- Experts are advising against it, considering it very insecure at this moment



Australia

Australia has used internet voting in several elections in New South Wales since 2011.

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Canada

Canada has not conducted any online elections at the provincial or federal level, but internet voting has been used in local elections.

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Estonia

Estonia began an internet voting program in 2005.

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Finland

Finland explored the use of a kiosk-based online voting system.

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France

France conducted an online primary in 2014.

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Norway

Norway has experimented with internet voting systems.

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Other Countries

Other European countries have experimented with electronic or Internet voting and have elected to discontinue its use.

[MORE >](#)

References

- M. Bistarelli and S. Santancini. End-to-end voting with non-permissioned and permissioned ledgers. Journal of grid computing, March 2019.
- S. Nagaraj, G. Raju, and V. Srinath. Data encryption and authentication using public key approach. Procedia Computer Science (2015).
- International Conference on Computer, Communication and Convergence (ICCC 2015).
- B. P. Sloane Brakeville. Blockchain basics: Introduction to distributed ledgers. (June 2018)

Questions?